

$\min c^\top x$ subject to $Ax = b$, $x \geq 0$ where

$$A = \begin{bmatrix} & & \\ & & \\ & & \end{bmatrix}, \quad b = \begin{bmatrix} & \\ & \\ & \end{bmatrix}, \quad c = \begin{bmatrix} & \\ & \\ & \end{bmatrix}$$

$$\mathcal{B} = \left\{ \quad \right\}, \quad B = \begin{bmatrix} & & \\ & & \\ & & \end{bmatrix}, \quad c_B = \begin{bmatrix} & \\ & \\ & \end{bmatrix}, \quad \underline{Bx_B = b} \implies x_B = \hat{b} = \begin{bmatrix} & \\ & \\ & \end{bmatrix}$$

$$\mathcal{N} = \left\{ \quad \right\}, \quad N = \begin{bmatrix} & & \\ & & \\ & & \end{bmatrix}, \quad c_N = \begin{bmatrix} & \\ & \\ & \end{bmatrix}$$

$$\underline{B^\top y = c_B} \implies y = \begin{bmatrix} & \\ & \\ & \end{bmatrix} \implies \underline{\hat{c}_N = c_N - N^\top y} = \begin{bmatrix} & \\ & \\ & \end{bmatrix}$$

$\hat{c}_N \geq 0$?: stop, optimum

$$\hat{c}_N \xrightarrow[\text{of min}]{\text{index from } \mathcal{N}} t = \boxed{\quad} \xrightarrow{\text{entering}} \underline{B\hat{A}_t = A_t} \implies \hat{A}_t = \begin{bmatrix} \hat{a}_{1,t} \\ \vdots \\ \hat{a}_{m,t} \end{bmatrix} = \begin{bmatrix} & \\ & \\ & \end{bmatrix}$$

$\hat{A}_t \leq 0$?: stop, unbounded

$$\left\{ \frac{\hat{b}_i}{\hat{a}_{i,t}} \right\} = \left\{ \quad \right\} \xrightarrow[\text{min over } \hat{a}_{i,t} > 0]{\text{index from } \mathcal{B} \text{ of}} s = \boxed{\quad} \xrightarrow{\text{leaving}}$$

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$\hat{c}_N \geq 0$?: stop, optimum

\hat{c}_N

\rightarrow

index from \mathcal{N} of min

$t = \boxed{\quad}$

entering

$B\hat{A}_t = A_t \implies \hat{A}_t = \begin{bmatrix} \hat{a}_{1,t} \\ \vdots \\ \hat{a}_{m,t} \end{bmatrix} = \begin{bmatrix} & \\ & \end{bmatrix}$

$\hat{a}_{1,t}$

\vdots

$\hat{a}_{m,t}$

\rightarrow

index from \mathcal{B} of min over $\hat{a}_{i,t} > 0$

$s = \boxed{\quad}$

leaving

$\hat{a}_{i,t}$

$\hat{A}_t \leq 0$?: stop, unbounded

$\left\{ \frac{\hat{b}_i}{\hat{a}_{i,t}} \right\} = \left\{ \quad \right\}$

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\vdots

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\rightarrow

index from \mathcal{B} of min over $\hat{a}_{i,t} > 0$

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$\hat{a}_{i,t}$

$\hat{A}_t \leq 0$?: stop, unbounded

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