

## Homework #1

Due Wednesday 19 January, 2022 at 11:59pm.

Submit as a single PDF by using Gradescope, via the course Canvas site  
[canvas.alaska.edu/courses/7017](https://canvas.alaska.edu/courses/7017)

Problems from the textbook (Strang, *Intro Linear Algebra*, 5th ed. 2016) will be graded for completion, while the “P” Problems will be graded for correctness. Answers/solutions to Textbook Problems are linked at  
[bueler.github.io/math314/resources.html](https://bueler.github.io/math314/resources.html)

*Put these Textbook Problems first on your PDF, in this order.*

**from Problem Set 1.1, pages 8–10:** # 2, 6, 8, 11, 13, 22, 31

**from Problem Set 1.2, pages 18–21:** # 1, 2, 3, 4, 6, 14, 21, 34

*Put these “P” Problems next on your PDF, in this order.*

- P1.** If  $\mathbf{v} - \mathbf{w} = \begin{bmatrix} 4 \\ 1 \end{bmatrix}$  and  $\mathbf{v} + \mathbf{w} = \begin{bmatrix} 3 \\ 2 \end{bmatrix}$ , compute and draw the vectors  $\mathbf{v}$  and  $\mathbf{w}$ .
- P2.** What linear combination  $c \begin{bmatrix} 4 \\ 1 \end{bmatrix} + d \begin{bmatrix} 3 \\ 2 \end{bmatrix}$  produces  $\begin{bmatrix} 7 \\ 8 \end{bmatrix}$ ? Express this question as two equations for the coefficients  $c$  and  $d$ , and find  $c, d$ .
- P3.** Two opposite corners of a unit cube in 4 dimensions are  $(0, 0, 0, 0)$  and  $(1, 1, 1, 1)$ . All corners have coordinates that are either 0 or 1. How many corners are there? How many edges? How many “3D faces”, which are themselves 3-dimensional cubes?
- P4.** Find nonzero vectors  $\mathbf{v}$  and  $\mathbf{w}$  which are perpendicular to  $(-1, 0, 1)$  and to each other.
- P5.** True or false? If true give an explanation. If false give a counterexample:
- If  $\mathbf{u}$  is perpendicular to  $\mathbf{v}$  and  $\mathbf{w}$ , then  $\mathbf{u}$  is perpendicular to  $2\mathbf{v} - \mathbf{w}$ .
  - If  $\mathbf{u}$  and  $\mathbf{v}$  are perpendicular unit vectors then  $\|\mathbf{u} + \mathbf{v}\| = \sqrt{2}$ .
  - If  $\mathbf{u} = (-1, 1, -1)$  is perpendicular to  $\mathbf{v}$  and  $\mathbf{w}$ , then  $\mathbf{v}$  is parallel to  $\mathbf{w}$ .
- P6.** Draw a parallelogram with sides  $\mathbf{v}$  and  $\mathbf{w}$ . Then show that the squared diagonal lengths  $\|\mathbf{v} + \mathbf{w}\|^2 + \|\mathbf{v} - \mathbf{w}\|^2$  add to the sum of the four squared side lengths, that is,  $2\|\mathbf{v}\|^2 + 2\|\mathbf{w}\|^2$ .