## Worksheet: Volumes by discs or washers.

Do these calculations with a group, if possible.
A. Sketch the region bounded by the given curves:

$$
y=2 x^{3}, \quad x=1, \quad y=0 .
$$

Now sketch a typical slice and find the volume when the region is rotated around the $y$-axis.
B. Sketch the ellipse $x^{2}+9 y^{2}=9$. Rotate it around the $x$-axis, sketch a typical slice, and find the volume of the resulting rugby-ball-like ellipsoid.
C. Sketch the region bounded by the given curves:

$$
y=\ln x, \quad x=2, \quad y=0 .
$$

Now sketch a typical slice and find the volume when the region is rotated around the $y$-axis.

