Math 422 Intro to Complex Analysis (Bueler)

February 12, 2008

## Assignment #4

DUE Wednesday 20 February, 2008

Exercises on pages 53–54 of Brown & Churchill: # 1c, 2ab, 3c, 4, 5, 8, 9

Exercises on pages 59–60 of BROWN & CHURCHILL: # 1bd, 2, 3, 4, 6b, 8abc

**Exercise C4**. *Theory question.* Identify a single limit which, once proven, will allow us to show the famous rule for differentiating the exponential of a complex input:

 $f(z) = e^z \implies f'(z) = e^z.$ 

What algebraic fact must be true of the exponential function to get this result?

**Exercise C5**. *Theory question.* Identify a single limit which, once proven, will allow us to show the famous rule for differentiating the sine of a complex input:

 $f(z) = \sin(z) \implies f'(z) = \cos(z).$ 

What trigonometric identity (identities) must be true to get this result?