

1. Find the derivative of $f(x) = (x + x^2)(x^{-1} + 3)$ in two ways:

(i) by the product rule:

(ii) by first expanding the product:

2. Differentiate.

(a) $y = \frac{\sqrt{x}}{2+x}$

(b) $g(x) = (\pi^{1/2} + 5\sqrt{x})e^x$

(c) $f(x) = \frac{ax+b}{cx+d}$

3. If $h(2) = 4$ and $h'(2) = -3$, find

$$\frac{d}{dx} \left(\frac{h(x)}{x} \right) \Big|_{x=2}$$

4. Consider these facts:

- $\csc x = 1/\sin x$
- $\cot x = \cos x/\sin x$
- $(\sin x)' = \cos x$

Use the quotient rule and the above facts to show that

$$\frac{d}{dx} (\csc x) = -\csc x \cot x$$

5. Differentiate $f(\theta) = \theta \cos \theta \sin \theta$.